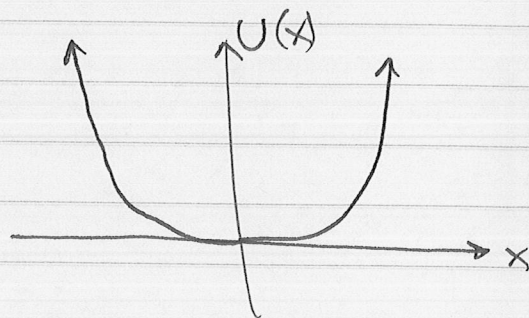


13.26 Mass m on x -axis with $F_x = -kx^3$, $k > 0$.

Note that $F_x = -\frac{dU}{dx}$ with $U(x) = \frac{k}{4}x^4$.

$$T = \frac{1}{2}m\dot{x}^2$$

$$U = \frac{k}{4}x^4$$

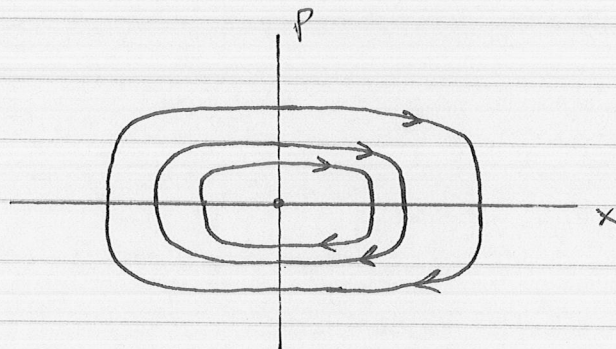


$\rightarrow H = T + U$ (coords. are "natural")

$$= \frac{1}{2}m\dot{x}^2 + \frac{1}{4}kx^4$$

$$= \frac{p^2}{2m} + \frac{1}{4}kx^4 \quad (p = m\dot{x} = \frac{\partial L}{\partial \dot{x}})$$

Since $H(x, p)$ is not explicitly time-dependent,
 $H = \text{const.}$ for any motion.



Phase space orbits are roughly elliptical (but flatter at sides and top) ... motion is periodic, corresponding to oscillation about equilibrium at $x=0$.