

**MATH 211 – Answers to Review Problems**  
30 Nov. 2007

1.  $54.7^\circ$
- 2.
3.  $(\frac{2}{3}, -\frac{1}{3}, \frac{2}{3})$
- 4.
5.  $35.3^\circ$
- 6.
- 7.
- 8.
9.  $\mathbf{r}(t) = (t, t^2, \frac{1}{2}t^2)$
10.  $\mathbf{r}(t) = (3 \cos t, \frac{3}{\sqrt{2}} \sin t, \frac{3}{\sqrt{2}} \cos t)$
11. a)  $t = \pm 2$ ;  $(x, y) = (4, 0)$     b)  $53.13^\circ$
12.  $2x + y + 3z = 8$
13.  $t = 8$ ;  $(8, 28, -80)$
14.  $\mathbf{r}(s) = (2, 0, 1) + s(2, 2, 1)$ ;  $2x + 2y + z = 5$
15.  $\mathbf{T} = (1, 0, 0)$  at  $(0, 0, 0)$ ;  $\mathbf{T} = \frac{1}{\sqrt{14}}(1, -2, 3)$  at  $(-1, 1, -1)$ ;  $\mathbf{T} = \frac{1}{\sqrt{161}}(1, 4, 12)$  at  $(2, 4, 8)$
- 16.
17.  $4\sqrt{13}\pi$
18. 57
19. a)  $\mathbf{T}(2) = \frac{1}{\sqrt{5}}(2, 1, 0)$ ;  $\mathbf{N}(2) = \frac{1}{\sqrt{5}}(1, -2, 0)$
20. a)  $\frac{1}{\sqrt{3}}(1, 1, 1)$     b)  $\sqrt{3}(e - 1)$
- 21.
22. b) hottest:  $(4, -3)$     coldest:  $(-4, 3)$     c) i)  $(4, -3)$  ii)  $(-4, 3)$  iii)  $\pm(3, 4)$     d)  $-9^\circ\text{C/s}$     e)  $0^\circ\text{C/cm}$
23. b)  $\pm(1, 2)$
24. b) i)  $(1, 2)$     ii)  $\pm(2, -1)$
25. b)  $x + y = 4$
26. a)  $9/\sqrt{5}$     b)  $(1, 4)$ ;  $\sqrt{17}$     c)  $x + 4y - z = 3$
27.  $-3/\sqrt{6}$
28.  $\mathbf{r}(t) = (2, 1, 6) + t(1, \frac{1}{2}, 6)$
29.  $3x + 2y + 6z = 49$
30.  $2x + 4y + z = 14$

31.  $6x + 3y - z = 11$ ;  $\mathbf{r}(t) = (3, 1, 10) + t(6, 3, -1)$
- 32.
33. a) 2.02    b) 2
34. 143
35. a)  $28^\circ\text{C/s}$     b)  $\frac{28}{\sqrt{17}}^\circ\text{C/cm}$
36.  $3x + 5y - 4z = 18$
37.  $(4, 1, 2)$
38. a)  $(2, 2, -2)$     b)  $4/\sqrt{2} = 2\sqrt{2}$
39.  $\mathbf{r}(t) = (\frac{3}{2}, \frac{1}{2}, 0) + t(0, 1, 1)$
40. a)  $14^\circ\text{C/s}$     b)  $\sqrt{14}^\circ\text{C/cm}$
41. local min at  $(1, -2, -10)$ ; saddle at  $(-1, -2, 2)$
42. local max at  $(-1, -1, 12)$  and  $(1, 1, 12)$ ; saddle at  $(0, 0, 10)$
43. max=4, min=-4
44. max= $2\sqrt{37}$ , min= $-2\sqrt{37}$
45. 72
46.  $\frac{1134}{5}$
47.  $\frac{1}{4}$
48.  $(e^{3125} - 1)/10$
49.  $\frac{\pi}{4}(1 - e^{-4})$
50. 195